

## Formula Sheet for Final

- **Sample Mean**

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n x_i$$

- **Sample Variance**

$$s_x^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{X})^2$$

- **Covariance and Correlation Coefficient**

$$Cov(X, Y) = s_{xy} = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{X})(y_i - \bar{Y})$$

$$Corr(X, Y) = \rho_{xy} = \frac{Cov(X, Y)}{s_x s_y}$$

- **Expected Value**

$$\mu = E(X) = \int_{x_{min}}^{x_{max}} x f(x) dx$$

- **Variance**

$$\sigma^2 = Var(X) = \int_{x_{min}}^{x_{max}} (x - \mu)^2 f(x) dx$$

- **Uniform Distribution**

$$- f(x) = \begin{cases} \frac{1}{b-a} & a \leq x \leq b \\ 0 & \text{for all other } x \end{cases}$$

$$- \mu = \frac{a+b}{2}, \quad \sigma^2 = \frac{(b-a)^2}{12}$$

- **Normal distribution (notation)**

$$- X \sim N(\mu, \sigma^2) \text{ (notation)}$$

$$- Z = \frac{X-\mu}{\sigma} \sim N(0, 1)$$

- **Linear Combinations:  $W = aX \mp bY$ ,**

$$- \mu_W = a\mu_x \mp b\mu_y$$

$$- \sigma_W^2 = a^2\sigma_x^2 + b^2\sigma_y^2 \mp 2abCov(X, Y)$$

- **Sampling distribution of the sample means:**

$$\bar{X} \sim N\left(\mu, \frac{\sigma^2}{n}\right)$$

- **Chi-square:**

$$\chi_{n-1}^2 = \frac{(n-1)s^2}{\sigma^2}$$

- **C.I. for  $\mu$  ( $\sigma^2$  known):**

$$\bar{X} \mp z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

- **C.I. for  $\mu$  ( $\sigma^2$  unknown):**

$$\bar{X} \mp t_{n-1, \alpha/2} \frac{s}{\sqrt{n}}$$

- **C.I. for the population variance:**

$$LCL = \frac{(n-1)s^2}{\chi_{n-1, \alpha/2}^2}, \quad UCL = \frac{(n-1)s^2}{\chi_{n-1, 1-\alpha/2}^2}$$

- p-value: the smallest  $\alpha$  that you can reject  $H_0$ .
- Type-I error: the probability of rejecting a true  $H_0$ , denoted by  $\alpha$ .
- Type-II error: the probability of failing to reject a false  $H_0$ , denoted by  $\beta$ .
- Power of the Test =  $1 - \beta$